

## Sample exam AI Languages

### General remarks

- All exercises concern PROLOG
- All exercises will be judged on a scale from 1-10
- Hand in the questions together with your answers
- The exam is **not** an “open-book” exam; so you may not use books, readers, or notes.
- You may assume that commonly-used predicates (like the list predicates **insert**, **del**, **member**, etc.) are pre-defined. However, clearly indicate the predicates that you assume to be predefined.

1. Give a PROLOG program **range(M, N, Ns)** to generate a list of integers **Ns** in the range from **M** to **N**.
2. Define a PROLOG program **split(Numbers, Positives, Negatives)**, that splits a given list **Numbers** of integers into two new lists, the list of positive numbers (0 inclusive) **Positives** and the list of negative numbers **Negatives**. E.g., **split([3,-6,5,0,-2], Positives, Negatives)** holds if **Positives = [3,5,0]** and **Negatives = [-6,-2]**. Use cuts to make the program efficient.
3. Give a PROLOG predicate **disjoint(L1, L2)**, that is true if **L1** and **L2** are two lists without common elements.
4. The Ackermann function is defined as follows:

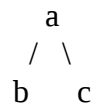
|                                                                                                                                     |
|-------------------------------------------------------------------------------------------------------------------------------------|
| <pre>ackermann(0, N) = N + 1; ackermann(M, 0) = ackermann(M - 1, 1); ackermann(M, N) = ackermann(M - 1, ackermann(M, N - 1)).</pre> |
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Give a PROLOG implementation of the Ackermann function.

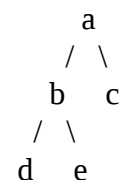
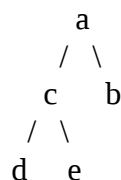
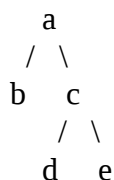
5. Define a PROLOG program **flatten(Xs, Ys)**, that holds if **Ys** is the list with elements that occur in the list of lists **Xs**. The elements of **Xs** can be elements themselves or can be lists, so elements in **Xs** may be nested arbitrarily deep. As an example: the goal **flatten([[a], [b], [c,a], [[b]]], [a,b,c,a,b])** is true.  
Hint: you best can use the standard function **atomic(X)**, that is true if **X** is an atom or a number.
6. Give a PROLOG program **subsum(Set, Sum, SubSet)** such that with **Set** a list of numbers, **SubSet** is a sublist of this list, and such that the sum of the numbers in **SubSet** equals **Sum**. For example:  

```
?- subsum([1,2,5,3,2], 5, Sub) .
Sub = [1,2,2];
Sub = [2,3];
Sub = [5];
Sub = [3,2];
no.
```

7. Give a PROLOG program **strangeSort** that sorts lists of positive integers as follows: the first element of the sorted list is the smallest element, the second the largest element, the third the smallest-but-one, the fourth the largest-but-one, and so on. For example, given the list **[3,6,1,2,4,7,5]** the program should yield the sorted list **[1,7,2,6,3,5,4]**. You may choose the method to do this yourself.
8. Write a PROLOG program **uniqueMerge** that merges 2 sorted lists in sorted order, but omits duplicates. You may assume that the two input lists are sorted, and don't contain duplicates themselves. So: **uniqueMerge([2,3,5,7,8], [1,2,5,6,8], L)** is true if and only if **L = [1,2,3,5,6,7,8]**.
9. Suppose we represent a binary tree with the ternary functor **tree(Element, Left, Right)**, in which **Element** is the root element, and **Left** and **Right** the left and right subtrees. The empty tree is represented by the atom **void**. The tree



then is represented as **tree(a, tree(b, void, void), tree(c, void, void))**. Write a PROLOG program **binary\_tree(Tree)** that determines if the argument **Tree** is a binary tree. Next give a program **tree\_member(Element, Tree)** that determines if **Element** is an element in the tree **Tree**. Finally, write a program **isotree(Tree1, Tree2)**, that determines whether 2 trees **Tree1** and **Tree2** are isomorphic. [Two trees T1 and T2 are isomorphic if T2 can be obtained from T1 by re-ordering the branches. For example, in the next figure the first two trees are isomorphic; the third one not.]



10. Use **bagof** to implement a relation **cycles\_of(Graph, Cycles)**, that determines all cycles **Cycles** of a given graph **Graph**. A graph is represented as a list of edges, for example **[a-b, b-c, c-a, b-d, d-c]**.

Good luck.